

Calculation of thermodynamic properties of the phases in the Y–Ba–Cu–O system

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Abstract

Enthalpy, entropy, specific heat, melting point and associated enthalpy change are calculated for 34 different phases considered to exist in the Y–Ba–Cu–O system. Polynomial coefficients for expressing the reduced Gibbs energy are also listed. Theoretically evaluated data are compared with the standard enthalpies of formation from their elements of the known compounds: Y_2BaCuO_5 ; $YBa_2Cu_3O_y$; $BaCuO_2$; $Y_2Cu_2O_5$; $YCuO_2$.

INTRODUCTION

According to the data given in refs. 1–10, in the system Y–Ba–Cu–O other phases have been found, besides the known compounds $BaCuO_2$, Y_2BaCuO_5 , $Y_2Cu_2O_5$, $YCuO_2$ and $YBa_2Cu_3O_y$ (where y varies from 6 to 7) (Table 1).

Current data about phases are necessary to perform research based on thermodynamical simulation (TS) [11,12].

The purpose of this work is to estimate the thermodynamic and thermochemical properties of some phases, and to calculate their reduced Gibbs energies.

A comparison of calculated and experimental values of the properties of a number of substances has been made.

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TABLE 1

Phases in the system Y–Ba–Cu–O^a

| Phases | Ref. |
|--|------|
| Ba ₂ CuO ₃ , Ba ₃ CuO ₄ , Y ₂ Ba ₄ O ₇ , Y ₂ BaO ₄ | 1 |
| Y ₂ Ba ₄ O ₇ , Y ₂ Ba ₂ O ₅ , Y ₂ BaO ₄ , Y ₄ Ba ₃ O ₉ , Y ₃ BaCuO _{7.5} ^b | 2 |
| Ba ₂ CuO ₃ , Y ₂ BaO ₄ , Y ₂ Ba ₂ O ₅ , Y ₂ Ba ₄ O ₇ , YBa ₃ Cu ₃ O _{7.5} ^b | 3 |
| YBa ₂ Cu ₄ O ₈ ^c , Y ₂ Ba ₄ Cu ₇ O _{14+x} ^c | 4 |
| YBa ₃ Cu ₂ O _{6.5} ^b , Y ₂ BaO ₄ , Y ₂ Ba ₄ O ₇ | 5 |
| Ba ₂ CuO ₃ , Y ₂ BaO ₄ , Y ₄ Ba ₃ O ₉ , YBa ₄ Cu ₃ O _{8.5} ^b , YBa ₅ Cu ₂ O _{8.5} ^b , Y ₃ Ba ₈ Cu ₅ O _{17.5} ^b | 6 |
| Ba ₂ CuO ₃ , Ba ₃ CuO ₄ , Y ₂ CuO ₄ , Y ₂ BaO ₄ , Y ₂ Ba ₂ O ₅ , Y ₄ Ba ₃ O ₉ , Y ₂ Ba ₄ O ₇ , YBa ₂ Cu ₄ O ₈ , YBaCu ₂ O _{4.5} ^b , YBa ₄ Cu ₃ O _{8.5} ^b , YBa ₃ Cu ₂ O _{6.5} ^b , YBa ₄ Cu ₂ O _{7.5} ^b , YBa ₅ Cu ₃ O _{9.5} ^b , YBa ₃ Cu ₅ O _{5.5} ^b , YBa ₂ CuO _{4.5} ^b , Y ₃ Ba ₈ Cu ₅ O _{17.5} ^b , Y ₄ BaCu ₅ O ₁₇ ^b | 7 |
| Ba ₂ CuO ₃ , Ba ₂ Cu ₃ O _{5+q} , YBa ₄ Cu ₃ O _{8.5} ^b , YBa ₆ Cu ₃ O _{10.5} ^b , Y ₃ Ba ₈ Cu ₅ O _{17.5} ^b , Ba ₂ CuO ₃ , Ba ₃ CuO ₄ , Y ₂ BaO ₄ , Y ₂ Ba ₄ O ₇ , Y ₄ Ba ₃ O ₉ , YBa ₃ Cu ₃ O _{7.5} ^b | 8 |
| Y ₂ Ba ₃ Cu ₅ O _{11+q} , Y ₂ BaCu ₃ O _{7-q} , Y ₂ Ba ₄ Cu ₃ O _{8.5+q} ^b , YBa ₄ Cu ₃ O ₈ , Y ₃ Ba ₈ Cu ₅ O _{16.45} , YBa ₅ Cu ₂ O _{8.34} | 9 |
| Y ₂ BaO ₄ , Y ₂ Ba ₂ O ₅ , Y ₂ Cu ₂ O ₅ , YBa ₄ Cu ₃ O _{8.97} , Y ₃ Ba ₈ Cu ₅ O ₁₈ , YBa ₅ Cu ₂ O _{8.97} , Y ₃ Ba ₈ Cu ₅ O ₁₈ | 10 |

^a The existence of phases BaCuO₂, Y₂BaCuO₅, Y₂Cu₂O₅, YCuO₂ and YBa₂Cu₃O_y (where y varies from 6 to 7) is considered proved.

^b The oxygen content is calculated on the assumption that the cations of yttrium, barium and copper have valencies 3, 2 and 2 respectively.

^c Superconductors with $T_c = 80$ K (YBa₂Cu₄O₈) and 14–68 K (Y₂Ba₄Cu₇O_{14+x}) [5,13,14].

CALCULATIONS

Some preliminary explanations

In most papers [1–10] the oxygen index in compounds either is not estimated or is not mentioned. These indexes are calculated by proceeding from the valencies of yttrium, barium and copper, which are equal to 3, 2 and 2 respectively.

The algorithm of the program complex ASTRA [11] does not allow the use of formulae containing fractional numbers of atoms. We have therefore adjusted such numbers to integers wherever possible, and doubled the formulae of compounds whose oxygen index is, for example, 6.5 or 8.5, etc.

The estimation of the thermodynamic functions of the superconducting phases YBa₂Cu₄O₈ and Y₂Ba₄Cu₇O_{14+x} is of special interest. According to ref. 13 YBa₂Cu₄O₈ has a narrow range of oxygen content (7.85–8.1) and $T_c \approx 80$ K. Thus, the group of formulae with oxygen index 8 describes this phase well enough. According to ref. 14, compounds Y₂Ba₄Cu₇O_{14.3–15.02} are superconducting with $T_c = 14–68$ K. We had no possibility of describing these compounds by fractional oxygen indexes, so we estimated thermody-

namical functions for $\text{Y}_2\text{Ba}_4\text{Cu}_7\text{O}_{14}$ (non-SC phase) and $\text{Y}_2\text{Ba}_4\text{Cu}_7\text{O}_{15}$ (SC phase).

According to various authors, some compounds have different oxygen indexes at equal cation compositions. We used those values of indexes that are found in several papers and/or obtained from the most reliable experiments. For some phases, which in our opinion, have not been analysed correctly, we did not make calculations of thermodynamic functions.

Calculations of thermodynamic and thermochemical properties were performed by using the methods described in refs. 15 and 16. The temperature dependence of the reduced Gibbs free energy was calculated using the sub-program TERMS in ASTRA, in the form

$$\phi_n^* = y_1 + y_2(\ln x) + y_3x + y_4x^{-1} + y_5x + y_6x^2 + y_7x^3 \quad (1)$$

where y_i are numerical coefficients, $x = T \times 10^{-4}$ (T in K) (technical system of units).

Table 2 shows properties of 34 phases. For compounds 1–4 properties have been calculated previously [15]; for the remainder, these properties are given for the first time.

COMPARISON WITH LITERATURE

We consider it necessary to compare calculated properties with known literature values. Such a comparison was made for YCuO_2 , $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$ ($\text{Y}_2\text{Ba}_4\text{Cu}_6\text{O}_{13}$), $\text{YBa}_2\text{Cu}_3\text{O}_6$, $\text{YBa}_2\text{Cu}_3\text{O}_7$, BaCuO_2 , Y_2BaCuO_5 and $\text{Y}_2\text{Cu}_2\text{O}_5$, mainly of standard enthalpies of formation from their elements. For the other phases we did not find any data about properties.

In a number of papers, the standard enthalpies of formation from oxides ($\Delta H_{298, \text{oxide}}^\circ$) were measured; conversion of those values to the enthalpies of formation from the elements was performed by the equation

$$\Delta H_{298}^\circ(i) = \Delta H_{298, \text{oxide}}^\circ(i) + \sum_{n=2} \Delta H_{298}^\circ(\text{oxide}) \quad (2)$$

$\text{YBa}_2\text{Cu}_3\text{O}_7$ (123-O₇): Standard enthalpy of formation from elements

The design value is $662.3 \text{ kcal mol}^{-1}$. In ref. 16 it is quoted as $-663.6 \text{ kcal mol}^{-1}$. An approximation of data from ref. 17 made in ref. 18 gives the value of $-651.3 \text{ kcal mol}^{-1}$. Averaging various data from ref. 18 leads to a value of $-650.0 \text{ kcal mol}^{-1}$. Refs. 19 and 20 give values of -645.4 and $-638.9 \text{ kcal mol}^{-1}$, respectively. In ref. 21 $\Delta H_{298, \text{oxide}}^\circ(123\text{-O}_7) = -45.48 \text{ kcal mol}^{-1}$ (in oxygen).

TABLE 2

Design values of thermodynamical and thermochemical properties of some superconducting and concomitant phases in the system Y-Ba-Cu-O

| No. | Phase | $-\Delta H_{298}^{\circ}$ (kcal mol ⁻¹) | S_{298}° (cal K ⁻¹ mol ⁻¹) | $H_{298}^{\circ} - H_0^{\circ}$ (cal mol ⁻¹) | $C_p = a + b(10^{-3})T - c(10^{-5})T^2$ | | | T_{melt} (K) | ΔH_{melt} (cal mol ⁻¹) | $\Delta C_{p,\text{melt}}$ (cal K ⁻¹ mol ⁻¹) |
|-----|--|--|--|---|---|-------|-------|--------------------------|--|---|
| | | | | | a | b | c | | | |
| 1 | YBa ₂ Cu ₃ O ₇ | 662.3 | 78.12 | 12297 | 72.26 | 17.03 | 8.58 | 1503 | 41030 | 104.31 |
| 2 | YBa ₂ Cu ₃ O ₆ | 628.5 | 77.2 | 12433 | 66.0 | 12.61 | 3.76 | 1446 | 36440 | 90.3 |
| 3 | Y ₂ BaCuO ₅ | 659.8 | 53.9 | 8883 | 49.5 | 8.86 | 3.3 | 1545 | 29200 | 67.72 |
| 4 | BaCuO ₂ | 183.4 | 26.7 | 4250 | 21.88 | 5.84 | 1.48 | 1280 | 10750 | 31.36 |
| 5 | Ba ₂ CuO ₃ | 322.7 | 42.7 | 6068 | 33.0 | 6.72 | 1.62 | 1360 | 17140 | 45.21 |
| 6 | Ba ₃ CuO ₄ | 462.0 | 58.7 | 8233 | 44.0 | 9.28 | 1.92 | 1315 | 22090 | 60.28 |
| 7 | Y ₂ Ba ₄ O ₇ | 1010.3 | 91.3 | 13050 | 71.5 | 14.17 | 3.64 | 1400 | 38220 | 97.96 |
| 8 | Y ₂ BaO ₄ | 610.6 | 43.3 | 6499 | 38.5 | 6.65 | 3.01 | 1610 | 23670 | 52.75 |
| 9 | Y ₂ Ba ₆ Cu ₄ O ₁₃ | 1488.6 | 166.1 | 24278 | 137.5 | 25.50 | 8.50 | 1495 | 78490 | 188.38 |
| 10 | Y ₂ Ba ₂ O ₅ | 745.4 | 59.3 | 8693 | 49.5 | 9.0 | 3.15 | 1525 | 28820 | 67.82 |
| 11 | Y ₄ Ba ₃ O ₉ | 1357.2 | 102.6 | 15200 | 88.0 | 15.68 | 6.08 | 1555 | 52250 | 120.56 |
| 12 | YBa ₂ Cu ₄ O ₈ | 684.0 | 88.9 | 13548 | 82.5 | 13.35 | 7.20 | 1715 | 54020 | 113.03 |
| 13 | Y ₂ Ba ₄ Cu ₆ O ₁₃ | 1298.2 | 155.4 | 25330 | 137.5 | 25.4 | 4.25 | 1496 | 78540 | 188.38 |
| 14 | Y ₂ Ba ₄ Cu ₈ O ₁₅ | 1386.4 | 176.9 | 26691 | 159.5 | 26.97 | 13.05 | 1640 | 99880 | 218.52 |

| | | | | | | | | | | |
|----|---------------------------|--------|--------|-------|--------|-------|-------|------|--------|--------|
| 15 | $Y_2Ba_4Cu_7O_{14}$ | 1342.3 | 166.2 | 24988 | 148.5 | 25.11 | 14.85 | 1645 | 93270 | 203.45 |
| 16 | $Y_6Ba_{16}Cu_{10}O_{35}$ | 4099.0 | 444.9 | 65028 | 368.5 | 68.34 | 22.78 | 1495 | 210350 | 504.85 |
| 17 | Y_2CuO_4 | 520.5 | 38.0 | 5964 | 38.5 | 5.81 | 4.13 | 1840 | 27050 | 52.75 |
| 18 | $Y_2Ba_2Cu_4O_9$ | 931.4 | 102.1 | 15496 | 93.5 | 15.47 | 7.82 | 1680 | 59980 | 128.10 |
| 19 | $Y_2Ba_8Cu_4O_{15}$ | 1767.2 | 198.1 | 28629 | 159.5 | 30.45 | 8.99 | 1450 | 88310 | 218.52 |
| 20 | $Y_2Ba_{10}Cu_6O_{19}$ | 2134.0 | 251.5 | 36415 | 203.5 | 38.85 | 11.47 | 1450 | 112670 | 278.80 |
| 21 | $Y_2Ba_6Cu_2O_{11}$ | 1400.4 | 144.7 | 20840 | 115.5 | 22.26 | 6.3 | 1440 | 63500 | 158.24 |
| 22 | $Y_2Ba_4Cu_2O_9$ | 1121.8 | 112.7 | 16482 | 93.5 | 17.17 | 5.95 | 1510 | 53910 | 128.10 |
| 23 | $Y_2Ba_4Cu_7O_{15}$ | 1368.6 | 166.95 | 27500 | 151.3 | 30.89 | 13.32 | 1645 | 96726 | 216.34 |
| 24 | $Y_2Ba_9Cu_6O_{17}$ | 1855.4 | 219.3 | 32519 | 184.1 | 36.76 | 18.00 | 1276 | 88427 | 247.26 |
| 25 | $Y_4BaCu_5O_{12}$ | 1312.6 | 124.0 | 21706 | 119.3 | 25.89 | 10.64 | 1342 | 62000 | 164.95 |
| 26 | $Y_2Ba_6Cu_6O_{15}$ | 1576.8 | 187.4 | 28587 | 160.4 | 33.65 | 15.03 | 1266 | 77100 | 217.27 |
| 27 | $Y_2Ba_3Cu_5O_{11}$ | 1114.8 | 128.7 | 20723 | 114.64 | 25.55 | 10.08 | 1267 | 55875 | 157.38 |
| 28 | $Y_2Ba_{12}Cu_6O_{21}$ | 2412.6 | 283.3 | 40383 | 225.4 | 40.59 | 23.94 | 1519 | 130786 | 307.49 |
| 29 | $Y_2BaCu_3O_7$ | 748.0 | 75.3 | 12860 | 70.63 | 15.56 | 6.12 | 1309 | 35736 | 97.47 |
| 30 | $Y_2Ba_{10}Cu_4O_{17}$ | 2045.8 | 229.9 | 30553 | 181.09 | 31.97 | 21.79 | 1092 | 71090 | 231.45 |
| 31 | $Y_2Cu_2O_5$ | 526.3 | 48.7 | 7650 | 49.50 | 8.28 | 3.96 | 1500 | 28350 | 67.82 |
| 32 | $YCuO_2$ | 261.3 | 23.9 | 3944 | 22.0 | 3.91 | 1.49 | 1560 | 13100 | 30.04 |
| 33 | $Ba_2Cu_3O_5$ | 410.8 | 64.05 | 9910 | 53.29 | 1.648 | 3.968 | 1014 | 21294 | 74.87 |
| 34 | $Ba_3Cu_5O_8$ | 638.4 | 101.42 | 15810 | 84.57 | 2.712 | 5.952 | 1011 | 33970 | 119.81 |

Conversion by eqn. (2)

$$\begin{aligned} \Delta H_{298}^{\circ}(123-O_7) = & \Delta H_{298,oxide}^{\circ}(123-O_7) + 0.5\Delta H_{298}^{\circ}(Y_2O_3) \\ & + 1.5\Delta H_{298}^{\circ}(BaO) + 0.5\Delta H_{298}^{\circ}(BaO_2) + 3\Delta H_{298}^{\circ}(CuO) \end{aligned} \quad (3)$$

gives the value $-658.8 \text{ kcal mol}^{-1}$.

In the same paper, for an air atmosphere, $\Delta H_{298,oxide}^{\circ}(123-O_7) = -36.97 \text{ kcal mol}^{-1}$. Conversion by eqn. (3) leads to the value of $-650.2 \text{ kcal mol}^{-1}$.

According to ref. 8 the enthalpy of formation from oxides is $-16.71 \text{ kcal mol}^{-1}$. Calculation by eqn. (3) gives the value $-630.0 \text{ kcal mol}^{-1}$. Another possible way of estimating $\Delta H_{298}^{\circ}(123-O_7)$ is by eqn. (2).

In ref. 22 $\Delta H_{298}^{\circ}(Cu_2O_3)$ is calculated as $-84.9 \text{ kcal mol}^{-1}$. With the use of these data and the enthalpy of formation of $123-O_7$ from oxides, we can calculate $\Delta H_{298}^{\circ}(123-O_7)$ by the equation

$$\begin{aligned} \Delta H_{298}^{\circ}(123-O_7) = & \Delta H_{298,oxide}^{\circ}(123-O_7) + 0.5\Delta H_{298}^{\circ}(Y_2O_3) \\ & + 2\Delta H_{298}^{\circ}(BaO) + 2\Delta H_{298}^{\circ}(CuO) + 0.5\Delta H_{298}^{\circ}(Cu_2O_3) \end{aligned} \quad (4)$$

Conversion of data from refs. 8 and 21 by eqn. (4) leads to the values of $-654.4 \text{ kcal mol}^{-1}$ (in oxygen), $-645.9 \text{ kcal mol}^{-1}$ (in air) [21] and $-625.7 \text{ kcal mol}^{-1}$ [8].

The average of 11 values of $\Delta H_{298}^{\circ}(123-O_7)$ is $-646.7 \text{ kcal mol}^{-1}$, which differs from the calculated value by about 2.4%.

Standard entropy of formation from elements $S_{298}^{\circ}(123-O_7)$

The design value is $78.12 \text{ cal mol}^{-1} \text{ K}^{-1}$. According to data in refs. 9, $S_{298}^{\circ}(123-O_7) = 77.36$ or $76.92 \text{ cal mol}^{-1} \text{ K}^{-1}$. According to ref. 23, $S_{298}^{\circ}(123-O_7) = -76.9 \text{ cal mol}^{-1} \text{ K}^{-1}$.

Heat capacity at 298 K $C_p(298)$

The design value is $67.67 \text{ cal mol}^{-1} \text{ K}^{-1}$. According to refs. 9 and 23, values are 68.34 , 67.5 and $67.46 \text{ cal mol}^{-1} \text{ K}^{-1}$.

Value of $H_{298}^{\circ} - H_0^{\circ}$

According to calculation the value is $12297 \text{ cal mol}^{-1}$. According to refs. 9 and 23, -12250 , 12140 and $12146 \text{ cal mol}^{-1}$.

$Y_2Ba_4Cu_6O_{13}$ ($YBa_2Cu_3O_{6.5}$): Standard enthalpy of formation from elements

The design value is $-1298.2 \text{ kcal mol}^{-1}$. According to ref. 17 for the composition $123-O_{6.47}$, $\Delta H_{298}^{\circ} = -1277.4 \text{ kcal mol}^{-1}$ (after doubling). The

value according to ref. 19 is $-1280 \text{ kcal mol}^{-1}$. In ref. 24, $\Delta H_{298,\text{oxide}}^{\circ}(123\text{-O}_{6.5}) = -34.19 \text{ kcal mol}^{-1}$. After conversion by eqn. (2) and doubling, we obtain $-1275.6 \text{ kcal mol}^{-1}$.

YBa₂Cu₃O₆: Standard enthalpy of formation from elements

The design value is $-628.5 \text{ kcal mol}^{-1}$. An approximation of data from ref. 17, made in ref. 18, leads to the value of $-640.7 \text{ kcal mol}^{-1}$. Averaging of values in ref. 18, leads to the value of $-631.6 \text{ kcal mol}^{-1}$. According to data in ref. 9, $\Delta H_{298,\text{oxide}}^{\circ}(123\text{-O}_6) = -34.19 \text{ kcal mol}^{-1}$. Conversion by eqn. (2) gives the value $-621.4 \text{ kcal mol}^{-1}$.

BaCuO₂: Standard enthalpy of formation from elements

The design value is $-183.4 \text{ kcal mol}^{-1}$. According to refs. 9 and 25 $\Delta H_{298,\text{oxide}}^{\circ}(\text{BaCuO}_2) = -23.45$ and $-22.31 \text{ kcal mol}^{-1}$, respectively. Conversion by eqn. (2) gives the values -192.8 and $-191.7 \text{ kcal mol}^{-1}$, respectively. According to ref. 25, $\Delta H_{298}^{\circ}(\text{BaCuO}_2) = -192 \text{ kcal mol}^{-1}$.

In ref. 26 the standard enthalpies of formation from their elements of BaCuO_{2.05}, BaCuO_{2.095} and BaCuO₂ were estimated, as -190.6 , -193.5 and $-187.7 \text{ kcal mol}^{-1}$, respectively.

Melting points, according to calculations and data in ref. 27, are 1280 and 1223 K, respectively.

Y₂BaCuO₅: Standard enthalpy of formation from elements

The design value is $-659.8 \text{ kcal mol}^{-1}$. According to ref. 9, the enthalpy of formation from oxides is $-18.72 \text{ kcal mol}^{-1}$. Conversion by eqn. (2) gives the value $-643.5 \text{ kcal mol}^{-1}$. According to ref. 24, $\Delta H_{298}^{\circ}(\text{Y}_2\text{-BaCuO}_5) = -647.3 \text{ kcal mol}^{-1}$.

Melting points, according to calculations and data in ref. 27, are 1545 and 1423 K, respectively.

Y₂Cu₂O₅: Standard enthalpy of formation from elements

The design value is $-526.3 \text{ kcal mol}^{-1}$. According to ref. 9 $\Delta H_{298,\text{oxide}}^{\circ}(\text{Y}_2\text{Cu}_2\text{O}_5) = 13.38 \text{ kcal mol}^{-1}$. Conversion by eqn. (2) gives the value $-543 \text{ kcal mol}^{-1}$. According to the data in ref. 28 the enthalpy of formation is $549.3 \text{ kcal mol}^{-1}$. Melting points, according to calculations and data in ref. 27, are 1500 and 1423 K, respectively.

YCuO₂

Design values of ΔH_{298}° and S_{298}° are $-261.3 \text{ kcal mol}^{-1}$ and $23.9 \text{ cal mol}^{-1} \text{ K}^{-1}$. According to ref. 28, these values are $-255.9 \text{ kcal mol}^{-1}$ and $21.76 \text{ cal mol}^{-1} \text{ K}^{-1}$.

TABLE 3
Polynomial coefficients of reduced Gibbs energy^a

| No. | Substance | T (K) | Polynomial coefficients ^b | | | | |
|-----|--|-----------------------|--------------------------------------|----------------------|-----------------|-----------------------|--------------|
| | | | y_1 | y_2 | y_3 | y_4 | y_5 |
| 1 | YBa ₂ Cu ₃ O ₇ | 298–1503 1503–6000 | 260.307 326.156 | 76.4024 101.8 | -0.0054411 0 | 1.46744 0.1724 | 62.153 0 |
| 2 | YBa ₂ Cu ₃ O ₆ | 298–1446 1446–6000 | 241.434 307.582 | 66.0001 90.4202 | 0.0018804 0 | 0.65333 -0.7519 | 63.053 0 |
| 3 | Y ₂ BaCuO ₅ | 298–1545 1545–6000 | 173.807 222.359 | 49.5 67.8202 | -0.00165 0 | 0.736877 -0.431503 | 44.303 0 |
| 4 | BaCuO ₂ | 298–1280 1280–6000 | 79.116 105.043 | 21.8801 31.3602 | -0.00074 0 | 0.302628 -0.048904 | 29.203 0 |
| 5 | Ba ₂ CuO ₃ | 298–1360 1360–6000 | 122.722 156.658 | 33 45.21 | -0.00081 0 | 0.46081 -0.226014 | 33.5999 0 |
| 6 | Ba ₃ CuO ₄ | 298–1315 1315–6000 | 165.436 211.241 | 44.0001 60.28 | -0.00096 0 | 0.593534 -0.291609 | 46.403 0 |
| 7 | Y ₂ Ba ₄ O ₇ | 298–1400 1400–6000 | 264.725 337.519 | 71.5 97.96 | -0.00182 0 | 1.01077 -0.5215 | 70.853 0 |
| 8 | Y ₂ BaO ₄ | 298–1610 1610–6000 | 136.383 173.625 | 38.5 52.7502 | -0.0015054 0 | 0.62794 -0.3254 | 33.253 0 |
| 9 | Y ₂ Ba ₆ Cu ₄ O ₁₃ | 298–1495 1495–6000 | 499.287 635.915 | 137.5 188.3801 | -0.00425 0 | 2.06817 -1.0808 | 127.503 0 |
| 10 | Y ₂ Ba ₂ O ₅ | 298–1525 1525–6000 | 179.25 228.074 | 49.5 67.82 | -0.001575 0 | 0.75148 -0.4039 | 45.003 0 |
| 11 | Y ₄ Ba ₃ O ₉ | 298–1555 1555–6000 | 315.67 401.817 | 88.0001 120.5601 | -0.00304 0 | 1.37606 -0.7207 | 78.403 0 |
| 12 | YBa ₂ Cu ₄ O ₈ | 298–1715 1715–6000 | 288.211 366.026 | 82.5 113.0302 | -0.0036 0 | 1.4046 -0.7668 | 66.752 0 |
| 13 | Y ₂ Ba ₄ Cu ₆ O ₁₃ | 298–1496 1496–6000 | 491.00 627.384 | 137.5 188.3801 | -0.0021254 0 | 1.81991 -1.2932 | 127.003 0 |
| 14 | Y ₂ Ba ₄ Cu ₈ O ₁₅ | 298–1640 1640–6000 | 562.378 715.435 | 159.5001 218.5201 | -0.0065254 0 | 2.64168 -1.3735 | 134.852 0 |

| | | | | | | | |
|----|---------------------------|-----------|----------|----------|------------|-----------|---------|
| 15 | $Y_2Ba_4Cu_7O_{14}$ | 298-1645 | 523.573 | 148.5 | -0.0074254 | 2.53632 | 125.552 |
| | | 1645-6000 | 666.078 | 203.4502 | 0 | -1.2391 | 0 |
| 16 | $Y_6Ba_{16}Cu_{10}O_{35}$ | 298-1495 | 1337.839 | 368.4997 | -0.0113904 | 5.54637 | 341.7 |
| | | 1495-6000 | 1703.993 | 504.8498 | 0 | -2.8937 | 0 |
| 17 | Y_2CuO_4 | 298-1840 | 130.70 | 38.5 | -0.0020654 | 0.7153 | 29.052 |
| | | 1840-6000 | 166.028 | 52.7502 | 0 | -0.3737 | 0 |
| 18 | $Y_2Ba_2Cu_4O_9$ | 298-1680 | 328.076 | 93.5001 | -0.0039104 | 1.56781 | 77.352 |
| | | 1680-6000 | 417.025 | 128.1 | 0 | -0.8471 | 0 |
| 19 | $Y_2Ba_8Cu_4O_{15}$ | 298-1450 | 584.827 | 159.5 | -0.0044945 | 2.32709 | 152.253 |
| | | 1450-6000 | 745.045 | 218.52 | 0 | -1.2091 | 0 |
| 20 | $Y_2Ba_{10}Cu_6O_{19}$ | 298-1450 | 744.91 | 203.5 | -0.0057354 | 2.98021 | 194.253 |
| | | 1450-6000 | 949.324 | 278.8 | 0 | -1.5315 | 0 |
| 21 | $Y_2Ba_8Cu_2O_{11}$ | 298-1440 | 424.799 | 115.5 | -0.0031504 | 1.66816 | 111.303 |
| | | 1440-6000 | 541.19 | 158.2402 | 0 | -0.879 | 0 |
| 22 | $Y_2Ba_4Cu_2O_9$ | 298-1510 | 339.222 | 93.5 | -0.0029754 | 1.41401 | 85.853 |
| | | 1510-6000 | 431.791 | 128.1002 | 0 | -0.7493 | 0 |
| 23 | $Y_2Ba_4Cu_7O_{15}$ | 298-1645 | 530.499 | 151.3001 | -0.0066604 | 2.34289 | 154.453 |
| | | 1645-6000 | 692.706 | 216.3402 | 0 | -0.8911 | 0 |
| 24 | $Y_2Ba_8Cu_6O_{17}$ | 298-1276 | 660.899 | 184.1 | -0.009 | 3.00153 | 183.8 |
| | | 1276-6000 | 844.535 | 247.26 | 0 | -0.915612 | 0 |
| 25 | $Y_4BaCu_5O_{12}$ | 298-1342 | 410.124 | 119.3 | -0.005321 | 1.85654 | 129.45 |
| | | 1342-6000 | 537.398 | 164.95 | 0 | -0.627859 | 0 |
| 26 | $Y_2Ba_6Cu_6O_{15}$ | 298-1266 | 572.034 | 160.4 | -0.0075154 | 2.575 | 168.253 |
| | | 1266-6000 | 736.669 | 217.2702 | 0 | -0.7506 | 0 |
| 27 | $Y_2Ba_3Cu_5O_{11}$ | 298-1267 | 403.529 | 114.64 | -0.0050404 | 1.79568 | 127.753 |
| | | 1267-6000 | 525.873 | 157.3802 | 0 | -0.507 | 0 |
| 28 | $Y_2Ba_{12}Cu_6O_{21}$ | 298-1519 | 824.211 | 225.4 | -0.0119704 | 3.66221 | 202.953 |
| | | 1519-6000 | 1045.097 | 307.4902 | 0 | -1.7873 | 0 |
| 29 | $Y_2BaCu_3O_7$ | 298-1309 | 224.728 | 70.6301 | -0.0030604 | 1.09324 | 77.803 |
| | | 1309-6000 | 320.309 | 97.4702 | 0 | -0.3469 | 0 |
| 30 | $Y_2Ba_{10}Cu_4O_{17}$ | 298-1092 | 665.741 | 182.0901 | -0.0108954 | 3.24415 | 159.854 |
| | | 1092-6000 | 826.618 | 231.4502 | 0 | -0.5804 | 0 |

TABLE 3 (continued)

| No. | Substance | T (K) | Polynomial coefficients ^b | | | | |
|-----|--|-----------|--------------------------------------|----------|------------|---------|---------|
| | | | y_1 | y_2 | y_3 | y_4 | y_5 |
| 31 | Y ₂ Cu ₂ O ₅ | 298-1500 | 168.409 | 49.5001 | -0.0019804 | 0.87976 | 41.403 |
| | | 1500-6000 | 216.252 | 67.8202 | 0 | -0.1652 | 0 |
| 32 | YCuO ₂ | 298-1560 | 77.187 | 22.0001 | -0.0007454 | 0.32857 | 19.553 |
| | | 1560-6000 | 98.612 | 30.0402 | 0 | -0.2125 | 0 |
| 33 | Ba ₂ Cu ₃ O ₅ | 298-1014 | 195.304 | 53.2902 | -0.0019844 | 0.53707 | 82.405 |
| | | 1014-6000 | 260.632 | 74.8703 | 0 | -0.2122 | 0 |
| 34 | Ba ₃ Cu ₅ O ₈ | 298-1011 | 309.235 | 84.5702 | -0.0029764 | 0.85988 | 135.605 |
| | | 1011-6000 | 415.48 | 119.8103 | 0 | -0.3015 | 0 |

^a From eqn. (1) (in cal K⁻¹ mol⁻¹). ^b Coefficients y_6 and y_7 are equal to zero for all phases.

In general, calculated and measured properties show good agreement and suggest promising uses of these calculations of thermodynamic data.

Table 3 summarizes the coefficients y_i of the approximating polynomial ϕ_n^* in eqn. (1).

CONCLUSIONS

On the basis of analysis of data for the Y–Ba–Cu–O system 34 phases (stable, metastable or hypothetical) were chosen, and identified in it. Calculations were used to estimate ΔH_{298}° , S_{298}° , $H_{298}^\circ - H_0^\circ$, $C_p(T)$, T_{melting} and $\Delta H_{\text{melting}}$, in addition to the temperature dependence of the reduced Gibbs energy in the range 298–6000 K.

Calculated and experimentally measured properties of $\text{YBa}_2\text{Cu}_3\text{O}_7$, $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$, $\text{YBa}_2\text{Cu}_3\text{O}_6$, BaCuO_2 , Y_2BaCuO_5 , $\text{Y}_2\text{Cu}_2\text{O}_5$ and YCuO_2 are in satisfactory agreement.

The data presented can be found useful in the further classification of phase compatibilities [29] as well as of formation under non-equilibrium (interface curvature or stress) conditions [30].

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